Multi-Battle Contests: An Experimental Study

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Abstract
We examine behavior of subjects in simultaneous and sequential multi-battle contests, where each individual battle is modeled as an all-pay auction with complete information. In simultaneous best-of-three contests, subjects are predicted to make positive bids in all three battles, but we find that subjects often make positive bids in only two battles. In sequential contests, theory predicts sizable bids in the first battle and no bids in the subsequent battles. Contrary to this prediction, subjects significantly underbid in the first battle and overbid in subsequent battles. Consequently, instead of always ending in the second battle, contests often proceeds to the third battle. Finally, although the aggregate bid in simultaneous contests is similar to that in sequential contests, in both settings, subjects make higher aggregate bids than predicted. The observed behavior of subjects can be rationalized by a combination of multi-dimensional iterative reasoning and a non-monetary utility of winning.

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1. Introduction

In multi-battle contests, players expend resources in order to win a series of individual battles and the player who wins a certain pre-determined number of battles wins the overall contest and receives the prize. For instance, consider a competition between two firms for a patent. Each firm must allocate resources to R&D in order to advance the innovation and secure the patent, but only the first firm to complete all stages of development gets the patent, while the competitor gets nothing. Similarly, a commander needs to win a majority of the battles in order to win the war. Such multi-battle contests can be characterized along a number of different dimensions such as asymmetry in resources, asymmetry in objectives, number of battles, interdependency between battles, and the sequence of play. Over the years, significant theoretical advancements have been made in examining how these factors impact behavior, resulting in a number of interesting predictions in the fields of patent races (Dasgupta, 1986; Konrad and Kovenock, 2009), R&D competitions (Harris and Vickers, 1985, 1987), multi-unit auctions (Szentes and Rosenthal, 2003), sports championships (Szymanski, 2003), network security (Hausken, 2008; Levitin and Hausken, 2010), elections (Snyder, 1989; Klumpp and Polborn, 2006) and redistributive politics (Laslier, 2002; Roberson, 2008). However, the predictive power of these models is difficult to test using field data. Laboratory experiments, on the other hand, provide a controlled environment more conducive to collect direct empirical evidence.

This paper reports an experimental investigation of two theoretical models of a multi-battle contest by Szentes and Rosenthal (2003) and Konrad and Kovenock (2009). Their common
framework captures a contest environment wherein players allocate resources (bids) over three battles, and the player expending the highest bid wins the individual battle with certainty. Both models assume that the player who wins a majority (two out of three battles) wins the contest and gets the prize (minus his bids) while the loser gets nothing but must still pay her bids. Thus, each individual battle is an all-pay auction with complete information.\(^3\) In the literature, this is a popular method of modeling environments where outcome is deterministic and not influenced by random exogenous noise. The models mainly differ in the timing of battles: Szentes and Rosenthal’s model captures simultaneous multi-battle contest (players allocate resources in all three battles simultaneously) while Konrad and Kovenock’s model captures sequential multi-battle contest (players observe the outcome of the first battle before making the bid decision for the second battle, and so on). The expected level of total expenditure in both models is equal to the value of the prize, yielding players zero expected payoffs in equilibrium. However, the difference in the temporal sequencing of battles yields marked difference in the predicted bid behavior in individual battles. In case of simultaneous contest, players are predicted to make positive and symmetric bids in all three battles, with bids restricted by certain theoretical boundaries. In case of sequential contest, players are predicted to make sizable bids only in the first battle and (almost) no bids in the subsequent battles. Contrary to these theoretical predictions, we find that subjects in simultaneous best-of-three contests often make positive bids in only two, instead of all three, battles and they significantly overuse moderately high bids. In sequential contests, subjects significantly underbid in the first battle and overbid in subsequent battles. Consequently, instead of always ending in the second battle, contests often proceed to the third battle. Finally, although the aggregate bid in

\(^3\) An all-pay auction is a simultaneous move game in which each player must pay his bid (as opposed to winner-pay auction) and the highest bidder wins the contest with certainty (Hillman and Riley, 1989; Baye et al., 1996). An alternative formulation is the “lottery” or Tullock contest (1980) where outcome is probabilistic, i.e. the probability of winning a stage-battle is increasing in player’s own bid and decreasing in the other player’s bid.
simultaneous contests is similar to that in sequential contests, in both settings, subjects make higher aggregate bids than predicted.

The observed behavior of subjects can be rationalized by a combination of a multi-dimensional iterative reasoning (Arad and Rubinstein, 2012) and a non-monetary utility of winning (Sheremeta, 2010a, 2010b). The multi-dimensional iterative reasoning suggests that, instead of using the “best response,” subjects evaluate the “proper response” to the various features of strategies. This suggests that subjects first decide on their total expenditure across all three battles, and then the number of battles and the level of bids in each battle. This explains the non-equilibrium behavior across battles. At the same time, subjects derive a non-monetary utility from the act of winning itself, which explains aggregate overbidding.

The results of our experiment might be of particular interest for public policy on patents and innovation. Beginning with the seminal papers by Loury (1979) and Lee and Wilde (1980), patent races have been often stylized as a contest between firms investing in R&D efforts with the aim of securing the ultimate prize, a patent. However, the literature is mostly theoretical (e.g., Harris and Vickers, 1985, 1987; Baye and Hoppe, 2003) and the predictions rely heavily on a set of stringent assumptions making it difficult to establish its relevance to the real world patent races. For instance, our sequential multi-battle contest is predicted to be behaviorally similar to a single-battle all-pay contest since winning the first battle (or ε-preemption) is all that is needed to win the entire contest. Our experimental results, on the other hand, can reflect on the strategic interaction between competitors as the race unfolds – the loss in the first battle does not deter the competitor from engaging in subsequent battles, and therefore mimic the real world patent races more closely. Similar parallels can be made for the simultaneous multi-battle contests. Our experimental results are consistent with the management literature that advocates disciplined, strategically-focused
processes as opposed to the traditional 'spray and pray' or 'one size fits all' approach that emerges from the theoretical analysis (Bayus and Mehta, 1995). Since in practice it is often hard to identify patent races because firms may file for patents for reasons other than outperforming their rivals, there is severe scarcity of field studies. Our experiment provides both direct, even if minimal, test of the theory as well as the next best explanation for the observed counterfactual results. Our findings underscore the importance of continued empirical investigation of the theoretical models of multi-battle contests if they are to be applied to explain patent races and innovation.

The rest of the paper is organized as follows: In Section 2 we review the literature – both theoretical and experimental – on simultaneous and sequential contests. In Section 3 we briefly describe the theoretical framework and the implied predictions for the experiment. Section 4 details the experimental design and procedures. Section 5 reports the results of the experiment and Section 6 concludes.

2. Literature Review

The theoretical literature on simultaneous multi-battle contests goes back to the original formulation of a Colonel Blotto game by Borel (1921). Colonel Blotto game is an archetype of the strategic multi-dimensional resource allocation problem – players must simultaneously allocate their resource endowment across n-battles, with the objective of maximizing the expected number of battles won. In each battle, the player who allocates the highest level of resources wins, and the payoff from the whole contest is contingent on the number of wins across all individual battles. The optimal strategy is a randomized allocation such that all battles are treated symmetrically and the marginal distribution of resources is essentially uniform in each battle (Roberson, 2006; Hart, 2008). Over the years, different variants of this game have been examined to address problems in
redistributive politics (Laslier, 2002; Roberson, 2008), military and systems defense (Kovenok and Roberson, 2015), vote buying (Myerson, 1993), package auctions (Milgrom, 2007) and political campaigns (Snyder, 1989; Klumpp and Polborn, 2006). The original constant-sum formulation of the game featured “use it or lose it” so that resources which are not allocated to one of the battles are forfeited and lose all value to the player. However, there are a number of applications where the unused resources retain their positive value and the resulting game is a non-constant-sum game. For example, resources not allocated to R&D may be used for advertising by the firms. Our *simultaneous* multi-battle contest is a non-constant-sum game of Szentes and Rosenthal (2003) in which the objective of each player is to win a majority (two out of three) of the battles.\(^4\) Szentes and Rosenthal refer to this as a simultaneous “pure chopstick” auction, where chopsticks are suggestive of identical objects that useless except in pairs. Although the focus of Szentes and Rosenthal (2003) is on a winner-pay first-price auction, they also state the results for an all-pay auction without the formal proof.\(^5\)

Experimental studies on *simultaneous* multi-battle contests are fairly recent, and mostly feature the constant-sum formulation. Avrahami and Kareev (2009) study a discrete version of Colonel Blotto game where players have asymmetric resources, while Chowdhury et al. (2013) test the continuous version under partners and strangers matching protocols. Arad (2012) examines a modified Colonel Blotto game where players have to choose from a small set of allocation decisions. A few studies have studied multi-battle contest games with asymmetric battles. Horta-Vallve and Llorente-Saguer (2010) and Avrahami et al. (2014) examine contests with additive objective function and differing valuation for battles. Both Duffy and Matros (2015) and Montero

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\(^4\) Other extensions of the game include the non-constant-sum formulation with proportional objective (Kvasov, 2007; Roberson and Kvasov, 2012) and asymmetric objective (Deck and Sheremeta, 2012; Kovenok and Roberson, 2015).\(^5\) Kovenock and Roberson (2012) provide a formal derivation of the equilibrium.
et al. (2016) examine contests with majoritarian objective function but differ in the way in which winner in each battle is determined (auction versus lottery contest success function). Despite the numerous differences in these studies a common result emerges: consistent with the theoretical predictions, most of the time players use a ‘complete coverage’ strategy when they have equal or more resources than the opponent, and use a ‘guerilla warfare’ strategy when they have fewer resources. Unlike these above-mentioned studies, we examine a simultaneous multi-battle contests with majoritarian objective function where both players and individual battles are symmetric, and players need not allocate all their resources to the contest (i.e., a non-constant-sum formulation).

The theoretical literature on sequential multi-battle contests originated with seminal work by Fudenberg et al. (1983). In their model, two identical firms simultaneously decide how much effort to put in R&D. After observing the result of the first battle, firms move on to the next battle. Fudenberg et al. find that firm which leads by two or more battles becomes a monopoly and the firm which lags behind drops out of the competition. That is, in equilibrium the expenditure across battles is “frontloaded.” Subsequent papers have investigated the sequence of the decisions (Klumpp and Polborn, 2006), asymmetry between players (Budd et al., 1993), impact of discount factors (Harris and Vickers, 1985, 1987), budget constraints (Leininger, 1991), and intermediate prizes (Gelder, 2014). Our sequential multi-battle contest is a dynamic game of Konrad and Kovenock (2009) with complete information where each battle is an all-pay auction.

Experimental studies on sequential multi-battle contests mostly feature elimination contests wherein players compete within their own groups by expending efforts, and the winner of

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6 In another related paper, Arad and Rubinstein (2012) examine behavior in a version of the Colonel Blotto game in which in the case of a tie neither of the players wins the battle. Thus, the standard constant-sum Colonel Blotto game is transformed into a non-constant-sum game due to possible ties. Holt et al. (2016) and Kovenock et al. (2016) examine behavior in a weakest-link game in which the attacker needs to win only one battle to win the contest but the defender needs to win all battles. Deck et al. (2016) report the results of a laboratory experiment testing theoretical predictions in a multi-battle contest with value complementarities among the battles, called the game of Hex.
each group proceeds to the second round (Parco et al., 2005; Amegashie et al., 2007; Sheremeta, 2010a, 2010b; Altmann et al., 2012). To the best of our knowledge, there are only three studies that examine the best-of-\( n \) sequential framework similar to ours. Zizzo (2002) studies a patent race similar to Harris and Vickers (1987) and finds that contestants compete more aggressively than predicted. Mago et al. (2013) examine the impact of intermediate prizes and luck on bidding behavior in a best-of-three contest. Irfanoglu et al. (2015) compare behavior in sequential versus simultaneous best-of-three contests. The main difference is that all these studies feature lottery contests as opposed to an all-pay auction. If the probability of winning a battle is contingent on player’s own bid divided by the sum of total bid expenditure as in the Tullock lottery contest, there is a unique pure strategy Nash equilibrium. However, if the selection of battle winner is deterministic as in the all-pay auction, the Nash equilibrium is in mixed strategies. Our study is the first to examine bidding behavior in a sequential multi-battle contest with deterministic all-pay contest success function.\(^7\)

3. Theoretical Model and Predictions

3.1. General Model

Assume that there are two risk-neutral players, \( X \) and \( Y \), competing in a series of battles for a commonly known prize value \( v \). The number of battles is \( n = 3 \). Let \( x_i \) and \( y_i \) be the amount of resources (bid) spent by players \( X \) and \( Y \) in battle \( i \). The contest success function is deterministic in the sense that player making the highest bid wins the battle with certainty. To win the overall contest and receive the prize, a player has to win a majority of the battles, i.e. at least \( k = (n +

\(^7\) There are some studies examining behavior in sequential multi-battle contests with asymmetric objectives (Deck and Sheremeta, 2012), indefinitely repeated contests (Deck and Sheremeta, 2016), and last stand behavior (Gelder and Kovenock, 2015).
1)/2 = 2 battles. The net payoff of $X$ (similarly to $Y$) is equal to the value of the prize (if he wins) minus the total bid he has spent during the contest:

$$\pi_X = \begin{cases} 
\nu - \sum_{i=1}^{n} x_i & \text{if } X \text{ wins the contest} \\
- \sum_{i=1}^{n} x_i & \text{otherwise}
\end{cases} \quad (1)$$

The battles in the contest proceed either simultaneously or sequentially. In the simultaneous multi-battle contest, players simultaneously choose bids $x_i$ and $y_i$ for all battles $i = 1, 2, 3$. Then, the winner of each battle is determined and the player who wins at least $k = 2$ battles wins the overall contest and obtains the prize. In the sequential multi-battle contest, players simultaneously choose bids $x_1$ and $y_1$ in battle 1. After determining the winner of battle 1, they move on to battle 2 where they choose $x_2$ and $y_2$. Players compete until one player has accumulated the required $k = 2$ victories.

### 3.2. Simultaneous Multi-Battle Contest

The solution to the simultaneous non-constant-sum multi-battle contest exists only for three battles and can be found in Szentes and Rosenthal (2003) and Kovenock and Roberson (2012). When $k = 2$ and $n = 3$, there is a unique, symmetric mixed strategy Nash equilibrium.\(^8\)

In the equilibrium, player $X$ makes a draw $(x_1, x_2, x_3)$ from a uniform probability measure on the three-dimensional surface defined by four points $(\frac{\nu}{2}, \frac{\nu}{2}, 0), (\frac{\nu}{2}, 0, \frac{\nu}{2}), (0, \frac{\nu}{2}, \frac{\nu}{2})$, and $(0,0,0)$; and then allocates $((x_1)^2, (x_2)^2, (x_3)^2)$ to the three battles according to the joint cumulative distribution function $F(x_1^2, x_2^2, x_3^2) = \frac{x_1 x_2}{\nu} + \frac{x_1 x_3}{\nu} + \frac{x_2 x_3}{\nu} - \frac{(x_1)^2 + (x_2)^2 + (x_3)^2}{2\nu}$. The marginal distribution in each battle is given by $F(x) = \sqrt{\frac{2x}{\nu}}$ with $x \in \left[0, \frac{\nu}{2}\right]$. The expected total bid

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\(^8\) Szentes and Rosenthal (2003) study a winner-pay first-price auction and only stated the results for an all-pay auction, while Kovenock and Roberson (2012) provide a formal derivation of the equilibrium.
expenditure by both players is equal to the value of the prize; and therefore, in equilibrium, the expected payoff to each player is $E(\pi_X) = E(\pi_Y) = 0$.

### 3.3. Sequential Multi-Battle Contest

The solution to the sequential multi-battle contest can be found in Konrad and Kovenock (2009). In contrast to the simultaneous contest, battles proceed sequentially, and both players simultaneously choose their bids in each battle. Players learn the outcome of the preceding battle before moving to the next battle. Note that the contest can end in two battles if the winner of battle 1 also wins battle 2. In the subgame perfect Nash equilibrium, in battle 1 player $X$ (similarly $Y$) uniformly randomizes according to the distribution function $F(x) = \frac{x}{v}$ with $x \in [0, v]$. The winner of battle 1 then proceeds to win the overall contest with probability one by incurring minimal bid expenditure in battle 2.\(^9\) Note that since only battle 1 is pivotal for determining the contest winner, sequential multi-battle contest of Konrad and Kovenock is behaviorally similar to a single battle all-pay auction. The expected total bid expenditure by both players is equal to the value of the prize; and therefore, in equilibrium, the expected payoff to each player is $E(\pi_X) = E(\pi_Y) = 0$.

\(^9\) The reason for minimal expenditure in battle 2 is as follows: In battle 1, players are symmetric in terms of the continuation values for the next battle, but in battle 2, the winner of battle 1 still has a strictly positive continuation value while the loser’s continuation value goes down to zero. Since the loser has no incentive to compete in battle 2 (the continuation value of winning in battle 3 is 0), he makes a bid of zero. Konrad and Kovenock (2009) assume in case of a tie in bid expenditures, winner is the player with a higher continuation value. This implies that the winner of battle 1 wins battle 2 and the overall contest without incurring any additional bid expenditure. In our experiment, the prize value is 100 francs and ties in all battles are determined by random coin flip. This implies that in battle 2, the winner of battle 1 should outbid the loser by an “epsilon” amount (0.1 francs in our experiment). Therefore, in battle 1 the prize is actually worth 99.9=100-0.1, implying that subjects in our experiment in battle 1 should randomize between 0 and 99.9. This, however, has no significant bearing on our experiment.
4. Experimental Design and Procedures

Within the multi-battle contest framework, we employ two treatments: *sequential* and *simultaneous*. In the simultaneous treatment, two players simultaneously decide on their bidding strategy across three battles, and the player who wins two battles wins the contest. In the sequential treatment, two players compete in a sequence of battles, and the first player to win two battles wins the contest. For our chosen parameters, the theoretical prediction for both treatments is shown in Table 1.

We ran a total of six experimental sessions (three for each treatment). Each session had 12 subjects, all of whom were recruited from undergraduate student population at Chapman University. No subject participated in more than one session, although some had participated in other economics experiments that were unrelated to this research. The computerized experimental sessions were programmed using z-Tree (Fischbacher, 2007). Throughout the session no communication between subjects was permitted and all choices and information were transmitted via computer terminals. Thus, all decisions were anonymous. Subjects were given the instructions, available in the Appendix, and the experimenter read the instructions aloud as subjects followed along on paper. Before the start of the experiment, subjects completed an online questionnaire that tested their comprehension of the instructions. The experiment started only after all subjects had answered the quiz questions, and explanations were provided for any incorrect answers.10

Each experimental session corresponded to 20 periods of play in one of the two treatments. In every period, the 12 subjects were randomly and anonymously placed into 6 groups with 2 players in each group. It was common knowledge that the valuation of prize was identical across all bidders and equal to 100 francs. Subjects were not allowed to bid more than 100 francs in any

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10 Prior to the main experiment, we also elicited subjects’ risk preferences by utilizing a series of 15 lottery choices, similar to Holt and Laury (2002).
battle and were informed that regardless of who wins the contest, all subjects would have to pay their bids. Subjects were also instructed that in each battle the bidder with the higher bid wins, and in case of a tie, winner is determined by a random coin flip. In the simultaneous treatment subjects were asked to make bids in each of the 3 battles simultaneously.\textsuperscript{11} After subjects submitted their bids, the computer displayed own bid, the opponent’s bid, the winner of each battle, the overall contest winner and the individual earnings that period. In the sequential treatment subjects participated either in two or three battles. At the end of each battle, the computer displayed own bid, the opponent’s bid, the winner of that battle. The period ended when one of the subjects in the group won two battles. At the end of each period subjects were randomly re-grouped to form a new 2-player group. The instructions explained the structure of the game in detail using a number of illustrative examples.

At the end of the experiment, 2 out of 20 periods were randomly selected for payment. The sum of the earnings for these 2 periods was exchanged at rate of 25 francs = $1. Additionally, all subjects received an initial endowment of $20 to cover potential losses. On average, subjects earned $21 each, which was paid anonymously and in cash, and earnings varied between $14 and $29. The experimental sessions lasted for about 60 minutes.

5. Results

5.1. Aggregate Results

Table 1 summarizes the equilibrium predictions and the aggregate results of the experiment. First notable feature of the data is that there is strong aggregate overbidding in both treatments. The average total bid in the simultaneous treatment is 69.2 and in the sequential

\textsuperscript{11} To keep the terminology neutral, in the instructions we describe the task as allocating tokens to three different boxes.
treatment it is 59.6, as compared to the theoretically predicted bid of 50. A standard Wald test, conducted on estimates of mixed-effects models, rejects the hypothesis that the average total bids in the simultaneous or sequential treatments are equal to the predicted bid (both p-values < 0.01).\textsuperscript{12} Such significant overbidding relative to the Nash prediction emerges with regularity in experimental literature on contests and all-pay auctions (see the review by Dechenaux et al., 2015).\textsuperscript{13}

**Result 1:** Average total bid in the simultaneous and sequential contests is significantly higher than predicted.

Figures 1, 2 and 3 show that overbidding is not reduced with experience. The coefficient on the time trend variable indicates that the bids increase in both the sequential and simultaneous treatment (both p-values < 0.01). To further elaborate on the overbidding behavior, following Baye et al. (1999), we employ two concepts of overdissipation. Baye et al. define *aggregate* overdissipation as the sum of bids by both players being greater than the value of the prize, and *individual* overdissipation as sum of bids by a single player being greater than the value of the prize. In both treatments, mixed strategy Nash equilibrium precludes the possibility of overdissipation in expectation: equilibrium aggregate dissipation is equal to the value of the prize (100), and there is no individual overdissipation since any bid greater than 100 would guarantee a negative payoff. However, since equilibrium involves nondegenerate mixed strategies, for

\textsuperscript{12} To support these conclusions we estimated a mixed-effects model for each treatment. We have 720 observations for each treatment (3 sessions \(\times\) 12 subjects \(\times\) 20 periods). The dependent variable in the regression is the total bid and the independent variables are a constant and a period trend. The model included a mixed-effects error structure, with subject and session as the random effects, to account for the multiple decisions made by each subject and random re-matching within a session. The standard Wald test conducted on estimates of a model, shows that the average bid in both treatments is significantly higher than predicted.

\textsuperscript{13} There are a number of explanations for over-dissipation in contests (see the reviews by Sheremeta, 2013, 2015). Some of the common explanations include non-monetary utility of winning (Sheremeta, 2010a, 2010b), mistakes (Sheremeta, 2011), misperception of probabilities (Shupp et al., 2013; Chowdhury et al., 2014), impulsivity (Sheremeta, 2016), and evolutionary bias (Mago et al., 2016).
particular realizations of the players’ mixed strategies, aggregate bids may exceed the value of the prize. That is, the game exhibits *probabilistic aggregate overdissipation*. Baye et al. show that for a single-battle all-pay auction, the probability of aggregate overdissipation is 0.5 when there are 2 players. In contrast to these predictions, Gneezy and Smorodinsky (2005) and Lugovskyy et al. (2010) find aggregate overdissipation at 0.84 and 0.88, respectively. In our experiment, the incidence of aggregate overdissipation is 0.83 in simultaneous treatment and 0.62 in sequential treatment. Finally, the average level of overbidding (relative to the expected prize) is 38.3% in the simultaneous treatment and 19.2% in the sequential treatment (can also be roughly inferred from Figures 1 and 2). Finally, note that *probabilistic individual overdissipation* is a dominated strategy since a player can guarantee a payoff of at least zero by bidding zero. In both treatments we find very few sporadic incidences where individual players bid more than the prize value of 100 (0.02 in simultaneous treatment and 0.07 in sequential treatment).\(^{14}\)

To make a direct comparison between simultaneous and sequential multi-battle contests, recall that according to the theoretical predictions of Szentes and Rosenthal (2003) and Konrad and Kovenock (2009) the expected level of total expenditure in both contests should be equal to the value of the prize. Therefore, both simultaneous and sequential multi-battle contests should result in the same aggregate bids. Figure 3 shows that the aggregate bids in both treatments over all 20 periods. A mixed-effects regression of total bid on the treatment dummy variables and a time trend indicates that the average bid in the simultaneous contest is higher than in the sequential contest (p-value = 0.03). However, the difference between the two contests becomes only

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\(^{14}\) Most of these incidences are subject specific. For example, in the simultaneous treatment, one subject is responsible for a third of the documented individual overdissipation. Our results are comparable to Gneezy and Smorodinsky (2006) who report incidence of individual overdissipation at 0.1.
marginally significant if we focus on the last 10 periods of the experiment (p-value = 0.06) and not significant when we restrict to only the last 5 periods of the experiment (p-value = 0.21).

**Result 2**: The aggregate bid in simultaneous contests initially is higher than in sequential contests, although there is convergence over time.

Next, we take a closer look at the individual battle behavior in both sequential and simultaneous contests.

### 5.2. Simultaneous Contest

The theoretical prediction for simultaneous contest is that in each battle players should randomize between 0 and 50 according to the cumulative distribution function \( F(x) = \frac{x}{\sqrt{50}} \), with an average bid of 16.7 in each battle. Figure 4 displays the empirical distribution of bids aggregated over all subjects and across all periods. In all three battles, the interval over which subjects randomize is between 0 and 50, with less than 5% of bids above 50. Thus, the aggregate behavior largely conforms to the equilibrium predictions. The overall distribution of bids is also remarkably similar in the three battles.

**Result 3**: In the simultaneous contest, bids fall within the predicted boundaries.

Although the main qualitative predictions of Szentes and Rosenthal (2003) model are supported, there are several interesting behavioral deviations from the theory. First, as stated in Result 1, there is significant overbidding, with bid in each battle averaging at 23.1 compared to the predicted level of 16.7. Figure 4 shows that instead of a concave distribution, bids are distributed according to a convex/linear cumulative distribution function. Second, there is evidence of positional order effects, i.e. the effect arising of the ordering of battles in the onscreen presentation. The average bid in battle 1 (24.4) is higher than the average bid in battle 2 (22.8) and
the average bid in battle 3 (21.9). Third, and most importantly, contrary to the theory, players do not employ ‘stochastic complete coverage.’ Figure 4 indicates that there is a mass point at 0 in each of the three battles, suggesting that subjects do not make any bids in a given battle around 20% of the time. In fact, there is pronounced bi-modality in subject choices, with subjects making either very small bids (bids less than or equal to 1 amount to 24.6% of the bids) or very large bids (bids greater than or equal to 30 amount to 42.6% of the bids). A closer look at the individual data shows that subjects make positive bids in all three battles only 62% of the time (instead of 100%), and they make positive bids in two out of three battles 35% of the time (instead of 0%). Furthermore, the choice of the number of battles is individual specific. We find that 61% of the subjects can be characterized as ‘equilibrium bidders’ (defined as subjects who allocate their resources across all three battles more than 60% of the time) and 28% as ‘guerilla bidders’ (defined as subjects who are more likely to focus their attention on two battles).

Result 4: In the simultaneous contest, subjects significantly overuse moderately high bids and 35% of the time they make positive bids in only two out of three battles (instead of all three).

It is important to emphasize, that such non-optimal behavior is costly. Given that others bid 0 in some battles, one can increase the chance of winning substantially by simply making a very cheap bid of 0.1. Therefore, error-based behavioral models, such as quantal response equilibrium (McKelvey and Palfrey, 1995), would not be a good explanation for Result 4. However, Result 4 can be rationalized by a multi-dimensional iterative reasoning proposed by Arad and Rubinstein (2012). They argue that in some games, including multi-battle contests, the feasible strategy space is so complex in structure that it is very difficult (if not impossible) for

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15 This echoes findings by Chowdhury et al. (2013) and Montero et al. (2016).
16 In discussing the winning strategies in Colonel Blotto games, Arad and Rubinstein (2012) point out that bid of 0 is non-optimal because that battle is likely to be lost or at most can achieve a tie. On the other hand, bidding a small amount may substantially increase the chance of winning.
human players to compute the “best response.” This forces players to evaluate the “proper response” to the various features (or “dimensions”) of strategies rather than focus on the “best response” strategies per se. The decision process entails that the player decides on each of the various dimensions of her strategy separately and then integrates her choices across these dimensions to formulate her overall strategy. The dimensions of strategy in the simultaneous multi-battle contest can, for instance, include total expenditure, the number of chosen battles, and the level of bids across chosen battles.17

In our data, we observe patterns that are consistent with a multi-dimensional iterative reasoning whereby subjects choose to focus on certain dimensions of strategy. For example, the total dissipation rate is very similar whether subjects bid in all three or in the chosen two battles. The average total bid across three battles is 69.2 and across two battles is 75.2. This suggests that even though the budget constraint is not binding, players decide on their total expenditure (a dimension of strategy) and it is fairly similar whether they bid on two or three battles. The fact that the aggregate bid is higher than predicted can be explained by another well-documented finding that in addition to monetary prize, subjects have a non-monetary utility of winning (Sheremeta, 2010a, 2010b; Price and Sheremeta, 2011, 2015; Cason et al., 2012, 2016).

Besides the total expenditure, another aspect of strategy dimension is allocation across individual battles. According to an iterative process described by Arad and Rubinstein (2012), “proper response” to bidding in all three battles is to “reinforce” two battles because more resources in each reinforced battle increases the likelihood of winning those battles and (given the majoritarian objective function) the overall contest. Consistent with this, we find that 35% of the

17 The dimensions of strategy, both in number and nature, can differ widely across players. Arad and Rubinstein (2012) acknowledge that identification of these elements can be ad-hoc and suggest common sense as a guiding principle in selecting the elements of strategic interest.
time subjects make bids in only two battles. The next iterative step is that if other players are focusing on a minimal winning set of battles, a player may be strictly better off by allocating some resources to the third battle. Accordingly, we find that when subjects make positive bids in all 3 battles, about 40% of the time the minimal bid is less than or equal to 1. Finally, we find homogenous allocation strategy to be a dominant method of bidding across battles: 58.9% of the time when subjects make positive bids in only two battles they choose the same bid across the two battles, and 59.3% of the time when subjects make positive bids in all three battles they choose the same bid across any two battles. Only 10.4% of the time subjects choose the strategy of spreading their resources equally across all three battles.

To summarize, in the simultaneous multi-battle contest there is no one “best response” strategy that would guarantee a win in all situations. Given the complexity and the size of the strategy space, it is plausible to assume that players bounded by their reasoning capabilities often use heuristics. We do not claim that multi-dimensional iterative reasoning explains behavior of all subjects; or in fact, there exists one single procedure that explains the decision process for all. However, multi-dimensional reasoning can explain why some subjects choose to use ‘guerilla warfare’ strategy by making positive bids in only two out of three battles or even a minimal bid in the third battle. In addition, a non-monetary utility of winning can explain why the aggregate

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18 Interestingly, the probability of winning the contest when subjects make positive bids in only two battles is 0.58 and when they make positive bids in all three battles is 0.48. This difference in the likelihood of winning is significant (p-value < 0.01). To support this conclusion we estimated a probit model, where the dependent variable is the probability of winning the overall contest and the independent variables are a constant, a period trend and a dummy variable of whether the subject made positive bids in only two battles or in all three battles.

19 It is important to emphasize that the ‘guerilla warfare’ strategy is also observed in other experiments on Blotto-type games (Deck and Sheremeta, 2012; Chowdhury et al., 2013; Deck et al., 2016; Kovenock et al., 2016; Montero et al., 2016). Kovenock et al. (2016), for example, report behavior consistent with stochastic ‘guerilla warfare’ strategy in the simultaneous weakest-link contest. They find that when the objective for one of the players (attacker) is to win only one battle, then such a player attacks a single battle 80% of the time (even when such behavior is not predicted by the theory). Montero et al. (2016) also find that subjects often use strategies that allocate resources to a subset of battlefields that is the minimum necessary for winning. In our multi-battle contest, each player needs to win only two out of three battles to win the overall contest. This entails that some players may randomly select and focus their bid expenditure on just two battles.
level of expenditure is significantly higher than predicted. Taken together, behavior of subjects in the simultaneous multi-battle contest can be rationalized by a combination of a multi-dimensional iterative reasoning and a non-monetary utility of winning.

5.3. Sequential Contest

Next we analyze individual battle bidding behavior in the sequential multi-battle contest. The theoretical prediction of Konrad and Kovenock (2009) is clearly rejected by the data, for all three battles. In battle 1, theory predicts that each player should uniformly randomize between 0 and 100, with an expected average bid of 50. Instead, subjects on average bid 16.7 in battle 1 (Table 1). Moreover, from Figure 5, it is clear that instead of a uniform distribution between 0 and 100, there are virtually no bids above 50 (less than 1% of bids are above 50). In battle 2, theory predicts that the loser of battle 1 should bid 0 and the winner should bid 0.1 (an “epsilon”). This theoretical prediction is also rejected by the data. Instead of bidding zero, loser of battle 1 bids 24.7, while winner of battle 1 bids 34.0. Finally, the subgame perfect equilibrium for battle 3 is equivalent to a simple all-pay auction with two symmetric players (since both players have won one battle each). Therefore, the equilibrium strategy in battle 3 is to randomize uniformly between 0 and 100, with the expected average bid of 50. Figure 5 shows that, instead, subjects randomize between 0 and 70, with the average bid of 35.7. Overall, contrary to prediction, bids in battles 2 and 3 are significantly higher than the bid in battle 1 (p-value < 0.01).\(^\text{20}\)

\(^{20}\) We estimated two mixed-effects models, where the dependent variable is the bid and the independent variables are a period trend and a dummy-variable for battle 2 (or 3). The mixed-effects panel structure included subject and session as the random effects to account for the multiple decisions made by each subject and random re-matching within a session. The estimation results show that the dummy-variable is positive and significant for both battles 2 and 3 (p-value < 0.01). When comparing bids in battle 1 and battle 2, we used all observations. However, when comparing bids in battle 1 and battle 3, we used only those observations where contest ended in three battles.
Result 5: In the sequential contest, subjects significantly underbid in the first battle and make significantly higher bids in the subsequent battles.

Note that in equilibrium, the sequential contest should never proceed to battle 3. This is because the loser of battle 1 should give up in battle 2, and thus the winner of battle 1 should win battle 2 with probability one. However, as indicated by Result 4, major competition happens not in battle 1 but in the subsequent battles. As a result, the contest proceeds to the third battle 38% of the time, instead of predicted 0%. Figure 2 displays the average bid in each battle over 20 periods of the experiment. It appears that the aggregate pattern of behavior does not change with experience. Moreover, in all periods, the bidding expenditure profile features a “hold-up”: successful participation in later battles requires substantial bids, and this makes it less attractive to allocate higher bids in the preliminary battles.

Result 6: In the sequential contest, instead of ending the contest in the second battle, contest proceeds to the third battle 38% of the time.

Theory also predicts that the winner of battle 1 wins the overall contest with absolute certainty. We find that the probability of battle 1 winner winning the overall contest is 0.8, which is significantly lower than the theoretical prediction of 1 (p-value < 0.01). This can be explained by the fact that the loss in battle 1 does not discourage the loser and he continues to bid positive amount in battle 2. Consequently, battle 1 winner continues his winning streak in battle 2 only 62% of time. In battle 3, theory predicts that both players are equally likely to win, and indeed, we find that winner of battle 1 wins the third battle 48% of the time.

Result 7: In the sequential contest, the likelihood of the winner of the first battle winning the overall contest is significantly less than predicted.
Results 5 to 7 indicate that the behavior of subjects in the sequential contest poses a challenge to the theoretical predictions of Konrad and Kovenock (2009). Since it cannot be explained using the best response framework, we provide behavioral explanations for the observed data that encompass both iterative reasoning and utility of winning.21

We begin by analysing behavior in battle 1. The data show that instead of a predicted average bid of 50, the average bid in battle 1 is 16.7. This significantly lower expenditure can be interpreted as a “proper response” (Arad and Rubinstein, 2012) to the observation that most of the competition occurs in later battles, as opposed to the predicted “frontloaded” expenditure pattern. Since successful participation in later battles requires substantial bids, it seems prudent to conserve resources in the preliminary battle. For instance, an expenditure of 50 (when other players are bidding smaller amounts) may win the player battle 1 with certainty, but it would restrict her strategy space in later battles and/or reduce her overall profit margin.

In battle 2, we find significant overbidding by both the loser and the winner of battle 1 – the loser of battle 1 bids 24.7 while the winner of battle 1 bids 34. Based on the assumption that subjects care only about their monetary prize, standard theory predicts that the loser of battle 1 will suffer from a dramatic decrease in his continuation value for the next battle, and accordingly will not bid a positive amount. However, if we incorporate winning as a component in the subject’s utility function (Sheremeta, 2010a, 2010b), the decline in continuation value for battle 2 is not so

21 It is important to emphasize that subjects’ behavior is not consistent with the subgame perfect equilibrium. Employing backward induction, consider that average bid in battle 3 is 35.7. This implies that subject’s expected payoff from the third battle is positive (0.5*100-35.7=14.3) and therefore, positive bid in the second battle are not entirely irrational. The extent of actual overbidding, however, is quite substantial. In the data, we find that 87% of the sum of bids in battles 1 and 2 are more than 14.3. Even focusing solely on battle 2, 74% of the bids exceed the rationalizable threshold of 14.3. Similarly, if we assume that subjects have correct expectation about the competition in battles 2 and 3, then they should not bid as much as predicted by the theory in battle 1. Since the average sum of bids in battles 2 and 3 is 42.9, it follows that subjects in battle 1 should behave as if the expected payoff was 7.1 (100*0.5-42.9=7.1). Again, we find that bids in battle 1 exceeding the rationalizable threshold of 7.1 account for 69.2% of the observations. Thus, neither backward nor forward induction can explain subjects’ behavior in the sequential multi-battle contest.
dramatic. In fact, the loser of battle 1 may not only have a non-monetary utility of winning battle 2, but may also expect to receive an additional utility from a possible win in battle 3. Such utility inherently transforms the game into a multi-battle sequential contest with intermediate prizes; and one of the fundamental theoretical results in the sequential contest with intermediate prizes is that “the player who is lagging behind may catch up, and does catch up with a considerable probability in the equilibrium” (Konrad and Kovenock, 2009, page 267). This explanation is consistent with our finding that the loser of battle 1 makes positive bid in battle 2, and thus wins 38% of the time in battle 2 and 20% of the time in the overall contest.

In battle 3, there is no overbidding – the average observed bid is 35.7 and the expected bid is 50. However, this underbidding in battle 3 is less surprising if we account for the extent of overbidding in battle 2. Subjects who get to battle 3 have already made positive bids in the previous two battles, and may choose to use a restricted strategy space if they are to make a positive profit (or if they have a specific budget constraint in mind). A mixed-effects regression shows that there is a negative relationship between bid in battle 3 and total bid expenditure in the previous two battles (p-value = 0.06). This reduced expenditure in battle 3 can be interpreted as a “proper response” in a multi-dimensional iterative reasoning framework. To account for the impact of previous battle expenditures, we also compute the empirical “proper bid” in battle 3 using individual subject data. Specifically, this proper bid is the difference between the expected prize value of 50 and the bids already incurred in battles 1 and 2. Under the premise of no individual overdissipation, subjects should not bid greater than the proper bid in battle 3. However, if the

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22 In an experimental test of multi-battle contests with lottery contest success function, Mago et al. (2013) also find that intermediate prizes lead to significantly higher dissipation by both players, and reduced probability of the contest ending in 2 rounds.

23 Battle 1 loser puts a significantly higher bid in battle 2 compared to battle 1 (p-value < 0.01). Nonetheless, bid in battle 2 by the winner of battle 1 is still significantly higher than the bid by the loser of battle 1 (34 versus 24.7, p-value < 0.01). Mago et al. (2013) refer to this as a "strategic momentum."
perceived value of the prize is greater than 50 (i.e., subjects have a non-monetary value of winning the contest) we may observe bids that are higher than the proper bid. Indeed, we find that 87.6% of the time subjects’ bids in battle 3 are greater than their proper bid, suggesting that both a multi-dimensional iterative reasoning and a non-monetary utility of winning are necessary to explain non-equilibrium behavior in sequential contests.

6. Conclusion

This paper examines behavior of subjects in simultaneous and sequential multi-battle contests where each component battle is an all-pay auction with complete information. Our experiment provides some support for the qualitative predictions of Szentes and Rosenthal (2003), i.e. bids in the simultaneous multi-battle contest fall within the predicted boundaries. However, instead of the ‘complete stochastic coverage’ strategy, subjects employ the ‘guerilla warfare’ strategy by having a significant mass point at zero in each battle. Specifically, 35% of the time subjects make positive bids in only two out of three battles (instead of all three) and also significantly overuse moderately high bids. In case of sequential contest, data are clearly inconsistent with the predictions of Konrad and Kovenock (2009). Theory predicts sizable bids in the first battle and no bids in the subsequent battles. Contrary to this prediction, subjects significantly underbid in the first battle and make substantially higher bids in the subsequent battles. As the result, instead of always ending in the second battle, contest proceeds to the third battle 38% of the time. Finally, in both simultaneous and sequential settings, subjects make higher aggregate bids than predicted. We identify possible behavioral explanations for the lack of support for the equilibrium predictions of each model that incorporate both multi-dimensional iterative reasoning and a non-monetary utility of winning.
Multi-battle contests are prevalent in many real life situations and are readily applicable to a number of important strategic environments (e.g., multi-unit auctions, R&D and patent races, network security, conflicts, sports championship series, elections, redistributive politics). Therefore, it is hardly surprising that there has been an increased interest in the literature on multi-battle contests and many significant theoretical advancements have been made over the past decade by prominent scholars across a range of disciplines. The predictive power of most of these models, however, has not been tested because of paucity of suitable field data. Our experimental findings emphasize the importance of empirical investigation of the theoretical models of multi-battle contests. We find that although neither model of the multi-battle contest predicts individual behavior accurately, qualitatively speaking, the static model of Szentes and Rosenthal (2003) is a better predictor than the dynamic model of Konrad and Kovenock (2009). We believe that this discrepancy in predictive power might be of interest to contest designers – both theorists and practitioners in the field. The result that early loss in the sequential multi-battle contest does not prompt the player to leave the field to its competitor can also be utilized to study how patent races spur innovation wars (Scotchmer, 2006). Similarly, the guerilla warfare strategy adopted by contestants in the simultaneous multi-battle contest may be harnessed in policy recommendations to avoid wasteful duplication of effort. Our aim is not to formulate a precise theory of choice in these situations, and instead we propose a reasoning of strategy dimensions that can shed light on various decision considerations that arises in a contest framework. Future theoretical research should focus on how to incorporate these behavioral considerations into formal models of multi-battle contests.

Our findings also contribute to the recent studies investigating behavior in Colonel Blotto games (e.g., Avrahami and Kareev, 2009; Chowdhury et al., 2013). Unlike these studies, which
find strong support for theory, we find that individual behavior significantly diverges from the theoretical predictions, both quantitatively (in terms of the magnitude of overbidding) and qualitatively (in terms of the strategies used). A possible explanation for these differences is that we examine non-constant-sum multi-battle contests which allow for overdissipation, while Colonel Blotto game studies examine constant-sum multi-battle contests where resource allocation is restricted. Another explanation is that we examine a majoritarian objective function (i.e., the player winning the best of three battles wins the overall contest), while Colonel Blotto game studies examine proportional objective function (i.e., each battle has its separate reward). Whether it is the non-constant-sum nature or the majoritarian objective function that drives the difference between our findings and the findings of previous Colonel Blotto game studies is also an interesting question for future research.

Our experiment points out several fruitful avenues for future theoretical research. Perhaps one of the most interesting ones pertains to the excessive use of the ‘guerilla warfare’ strategy in simultaneous multi-battle contests. What kind of behavioral considerations would produce the ‘guerilla warfare’ strategy, instead of the ‘complete stochastic coverage’ strategy, as an equilibrium strategy? Similarly, in case of sequential multi-battle contests, it would be important to understand the behavioral reasons why ‘frontloading’ bidding profile is rejected in the lab.
References


Table 1: Equilibrium predictions and actual behavior

<table>
<thead>
<tr>
<th>Treatments</th>
<th>Sequential</th>
<th>Simultaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prize, v</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Number of battles, n</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Equilibrium Actual</td>
<td>Equilibrium Actual</td>
</tr>
<tr>
<td>Expected bid in battle 1</td>
<td>50.0</td>
<td>16.7 (0.5)</td>
</tr>
<tr>
<td>Expected bid in battle 2 by battle 1 winner</td>
<td>0.1</td>
<td>34.0 (1.0)</td>
</tr>
<tr>
<td>Expected bid in battle 2 by battle 1 loser</td>
<td>0.0</td>
<td>24.7 (1.0)</td>
</tr>
<tr>
<td>Expected bid in battle 3</td>
<td>50.0</td>
<td>35.7 (1.0)</td>
</tr>
<tr>
<td>The probability of ending in battle 2</td>
<td>1.0</td>
<td>0.62 (0.02)</td>
</tr>
<tr>
<td>Expected average total bid</td>
<td>50.0</td>
<td>59.6 (1.3)</td>
</tr>
<tr>
<td>Expected payoff</td>
<td>0.0</td>
<td>-9.6 (1.8)</td>
</tr>
</tbody>
</table>

Standard error of the mean is in parenthesis. We do not find a difference between expected bid in battle 3 by winners and losers of battle 2. Therefore, we combine the data for the bids in battle 3.
Figure 1: Bids in each battle across all periods in the simultaneous treatment

Figure 2: Bids in each battle across all periods in the sequential treatment

Figure 3: Aggregate bids across all periods in the simultaneous and sequential treatment
Figure 4: Distribution of bids in the simultaneous treatment

Figure 5: Distribution of bids in the sequential treatment
GENERAL INSTRUCTIONS

This is an experiment in the economics of strategic decision making. Various research agencies have provided funds for this research. The instructions are simple. If you follow them closely and make appropriate decisions, you can earn an appreciable amount of money.

The experiment will proceed in two parts. Each part contains decision problems that require you to make a series of economic choices which determine your total earnings. The currency used in Part 1 of the experiment is U.S. Dollars. The currency used in Part 2 of the experiment is francs. These francs will be converted to U.S. Dollars at a rate of **25** francs to **1** dollar. You have already received a **$20.00** participation fee (this includes your show-up fee of **$7.00**). Your earnings from both Part 1 and Part 2 of the experiment will be incorporated into your participation fee. At the end of today's experiment, you will be paid in private and in cash. There are **12** participants in today's experiment.

It is very important that you remain silent and do not look at other people's work. If you have any questions, or need assistance of any kind, please raise your hand and an experimenter will come to you. If you talk, laugh, exclaim out loud, etc., you will be asked to leave and you will not be paid. We expect and appreciate your cooperation.

INSTRUCTIONS FOR PART 1

In this part of the experiment you will be asked to make a series of choices in decision problems. How much you receive will depend partly on chance and partly on the choices you make. The decision problems are not designed to test you. What we want to know is what choices you would make in them. The only right answer is what you really would choose.

For each line in the table in the next page, please state whether you prefer option A or option B. Notice that there are a total of **15 lines** in the table but only **one line** will be randomly selected for payment. Each line is equally likely to be selected, and you do not know which line will be selected when you make your choices. Hence you should pay attention to the choice you make in every line. After you have completed all your choices a token will be randomly drawn out of a bingo cage containing tokens numbered from **1 to 15**. The token number determines which line is going to be selected for payment.

Your earnings for the selected line depend on which option you chose: If you chose option A in that line, you will receive **$1**. If you chose option B in that line, you will receive either **$3** or **$0**. To determine your earnings in the case you chose option B there will be second random draw. A token will be randomly drawn out of the bingo cage now containing twenty tokens numbered from **1 to 20**. The token number is then compared with the numbers in the line selected (see the table). If the token number shows up in the left column you earn **$3**. If the token number shows up in the right column you earn **$0**.

While you have all the information in the table, we ask you that you input all your 15 decisions into the computer. The actual earnings for this part will be determined at the end of part 2, and will be independent of part 1 earnings.

<table>
<thead>
<tr>
<th>Decision no.</th>
<th>Option A</th>
<th>Option B</th>
<th>Please choose A or B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$1</td>
<td>$3 never</td>
<td><strong>$0</strong> if 1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>2</td>
<td>$1</td>
<td>$3 if 1 comes out of the bingo cage</td>
<td><strong>$0</strong> if 2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>3</td>
<td>$1</td>
<td>$3 if 1 or 2</td>
<td><strong>$0</strong> if 3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>4</td>
<td>$1</td>
<td>$3 if 1,2,3</td>
<td><strong>$0</strong> if 4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>5</td>
<td>$1</td>
<td>$3 if 1,2,3,4,</td>
<td><strong>$0</strong> if 5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>6</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5</td>
<td><strong>$0</strong> if 6,7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>7</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6</td>
<td><strong>$0</strong> if 7,8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>8</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7</td>
<td><strong>$0</strong> if 8,9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>9</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8</td>
<td><strong>$0</strong> if 9,10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>10</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9</td>
<td><strong>$0</strong> if 10,11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>11</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9,10</td>
<td><strong>$0</strong> if 11,12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>12</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9,10,11</td>
<td><strong>$0</strong> if 12,13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>13</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9,10,11,12</td>
<td><strong>$0</strong> if 13,14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>14</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9,10,11,12,13</td>
<td><strong>$0</strong> if 14,15,16,17,18,19,20</td>
</tr>
<tr>
<td>15</td>
<td>$1</td>
<td>$3 if 1,2,3,4,5,6,7,8,9,10,11,12,13,14</td>
<td><strong>$0</strong> if 15,16,17,18,19,20</td>
</tr>
</tbody>
</table>

INSTRUCTIONS FOR PART 2
YOUR DECISION

The second part of the experiment consists of 20 decision-making periods. The 12 participants in today’s experiment will be randomly re-matched every period into 6 groups with 2 participants in each group. Therefore, the specific person who is the other participant in your group will change randomly after each period. The group assignment is anonymous, so you will not be told which of the participants in this room are assigned to your group.

Each period consists of a maximum of three rounds. The period ends when one of the participants wins two of the three rounds ("best of three"). Thus, each period will consist of either two or three rounds. In each round, you and the other participant in your group will simultaneously make a bid (any number, including 0.1 decimal points). Your bid in each round cannot exceed 100 francs. The more you bid, the more likely you are to win a particular round. This will be explained in more detail later. The participant who is first to win two rounds receives the reward of 100 francs. Your total earnings depend on whether you receive the reward or not and how many francs you spent on bidding. An example of your decision screen is shown below in Figure 1:

Figure 1 – Decision Screen

CHANCE OF WINNING A ROUND

If you bid more than the other participant in a particular round you win that round with certainty. So, if you bid 30 francs in a particular round while the other participant bids 29.9 francs in the same round then the computer will chose you as the winner of that round. In case both participants bid the same amount in the same round, the computer determines randomly who wins that round. In case both participants bid zero, the computer determines randomly who wins the round.

YOUR EARNINGS

Your earnings depend on whether you receive the reward or not and how many francs you spent on bidding. The participant who is first to win two rounds receives the reward of 100 francs. Regardless of who receives the reward, both participants will have to pay their bids in each round. Thus, the period earnings will be calculated in the following way:

1. If the period lasted for only two rounds
   Earnings of the participant who won both rounds are =
   = 100 - (bid in round 1) - (bid in round 2)
   Earnings of the participant who won neither rounds are =
   = 0 - (bid in round 1) - (bid in round 2)

2. If the period lasted for three rounds
   Earnings of the participant who won two rounds are =
   = 100 - (bid in round 1) - (bid in round 2) - (bid in round 3)
   Earnings of the participant who won one round are =
   = 0 - (bid in round 1) - (bid in round 2) - (bid in round 3)

END OF THE ROUND
After both participants make their round bids, the computer will determine the winner of the round. Both participants will observe the outcome of the round – your bid, other participant’s bid and winner, as shown in Figure 2. Then they make bids in another round. This continues until one of the participants in the group wins two rounds.

**Figure 2 – Intermediate Screen**

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**END OF THE PERIOD**

The period ends when one of the participants in the group wins two rounds. At the end of the period, the computer will calculate your period earnings based on whether you received the reward or not and how many francs you spent on bidding in each round. Your earnings from that period will be reported on the outcome screen as shown in Figure 3. Once the outcome screen is displayed you should record your results for the period on your **Personal Record Sheet** under the appropriate heading. You will be randomly re-matched with a different participant at the start of the next period.

**Figure 3 – Outcome Screen**

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**END OF THE EXPERIMENT**

At the end of the experiment we will use the bingo cage to randomly select 2 out of 20 periods for actual payment. Depending on the outcome in a given period, you may receive either positive or negative earnings. You will sum the total earnings for these 2 periods and convert them to a U.S. dollar payment, as shown on the last page of your personal record sheet. Remember you have already received a $20.00 participation fee (equivalent to 500 francs). If your earnings from this part of the experiment are positive, we will add them to your participation fee. If your earnings are negative, we will subtract them from your participation fee.